

UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS  
General Certificate of Education Ordinary LevelCANDIDATE  
NAMECENTRE  
NUMBER

--	--	--	--	--

CANDIDATE  
NUMBER

--	--	--	--

**MATHEMATICS (SYLLABUS D)****4024/12**

Paper 1

**October/November 2013****2 hours**

Candidates answer on the Question Paper.

Additional Materials: Geometrical instruments

**READ THESE INSTRUCTIONS FIRST**

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

You may use a pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

**DO NOT WRITE IN ANY BARCODES.**Answer **all** questions.

If working is needed for any question it must be shown in the space below that question.

Omission of essential working will result in loss of marks.

**ELECTRONIC CALCULATORS MUST NOT BE USED IN THIS PAPER.**

The number of marks is given in brackets [ ] at the end of each question or part question.

The total of the marks for this paper is 80.

This document consists of **20** printed pages.

**ELECTRONIC CALCULATORS MUST NOT BE USED IN THIS PAPER**
*For  
Examiner's  
Use*

- 1 (a) Amy buys 3 drinks at \$1.86 each and 1 drink for \$2.04.  
She pays for the 4 drinks with a \$10 note.

How much change should she receive?

*Answer* \$ ..... [1]

- (b) \$180 is shared between Ali and Ben so that Ali's share : Ben's share = 4 : 5.

Find Ali's share.

*Answer* \$ ..... [1]

---

- 2 (a) Evaluate  $3\frac{1}{4} - 1\frac{4}{5}$ .

*Answer* ..... [1]

- (b) Evaluate  $3.01 \times 0.02$ .

*Answer* ..... [1]

---

3

$$f(x) = 2x - 6$$

3

(a) Evaluate  $f\left(-\frac{1}{2}\right)$ .

*Answer* ..... [1]

(b) Find  $f^{-1}(x)$ .

*Answer*  $f^{-1}(x) =$  ..... [1]

---

4 (a) A journey started at 0744 and finished at 1132.

How long, in hours and minutes, did the journey take?

*Answer* ..... hours ..... minutes [1]

(b) Arrange these values in order, starting with the smallest.

$\frac{4}{9}$        $\frac{2}{5}$       44%

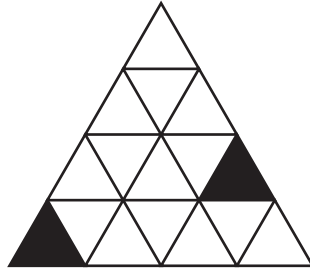
*Answer* ..... , ..... , ..... [1]  
*smallest*

---

*For  
 Examiner's  
 Use*

- 5 (a) In the diagram, two small triangles are shaded.

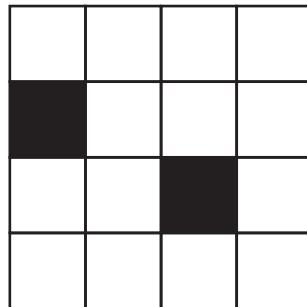
Shade one more small triangle, so that the diagram will then have one line of symmetry.



[1]

- (b) In the diagram, two small squares are shaded.

Shade two more small squares, so that the diagram will then have rotational symmetry of order 2.



[1]

- 6  $y$  is inversely proportional to  $x$ .

Given that  $y = 20$  when  $x = 2$ , find  $y$  when  $x = 5$ .

*Answer*  $y = \dots\dots\dots$  [2]

- 7 (a) Write the number 35 000 000 in standard form.

*Answer* ..... [1]

- (b) Giving your answer in standard form, evaluate  $\frac{4.2 \times 10^{-2}}{3 \times 10^4}$ .

*Answer* ..... [1]

---

- 8 Solve the equation  $\frac{3x+1}{2} - \frac{x}{3} = 1$ .

*Answer*  $x =$  ..... [2]

---

For  
Examiner's  
Use

- 9 By making suitable approximations, estimate the value of  $\frac{\sqrt{35.78} \times \sqrt[3]{1005}}{0.3012}$ .  
Show clearly the approximate values you use.

Answer ..... [2]

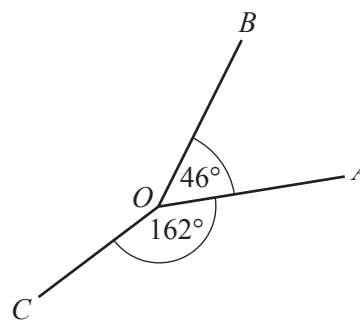
---

- 10 Find one value of  $x$  that satisfies both  $x > 4$  and  $17 - 4x > 2 - x$ .

Answer ..... [2]

---

- 11 In the diagram,  
 $\hat{A}OB = 46^\circ$ , correct to the nearest degree,  
 $\hat{A}OC = 162^\circ$ , correct to the nearest degree.



- (a) Write down the lower bound for  $\hat{A}OB$ .

Answer ..... [1]

- (b) Find the lower bound for  $\hat{B}OC$ .

Answer ..... [2]

---

12 (a) Evaluate  $\left(\frac{5}{3}\right)^{-2}$ .

Answer ..... [1]

(b) Simplify  $\left(\frac{9}{t^6}\right)^{\frac{1}{2}}$ .

Answer ..... [1]

(c) Simplify  $\frac{2x^3y}{6xy^2}$ .

Answer ..... [1]

For  
Examiner's  
Use

---

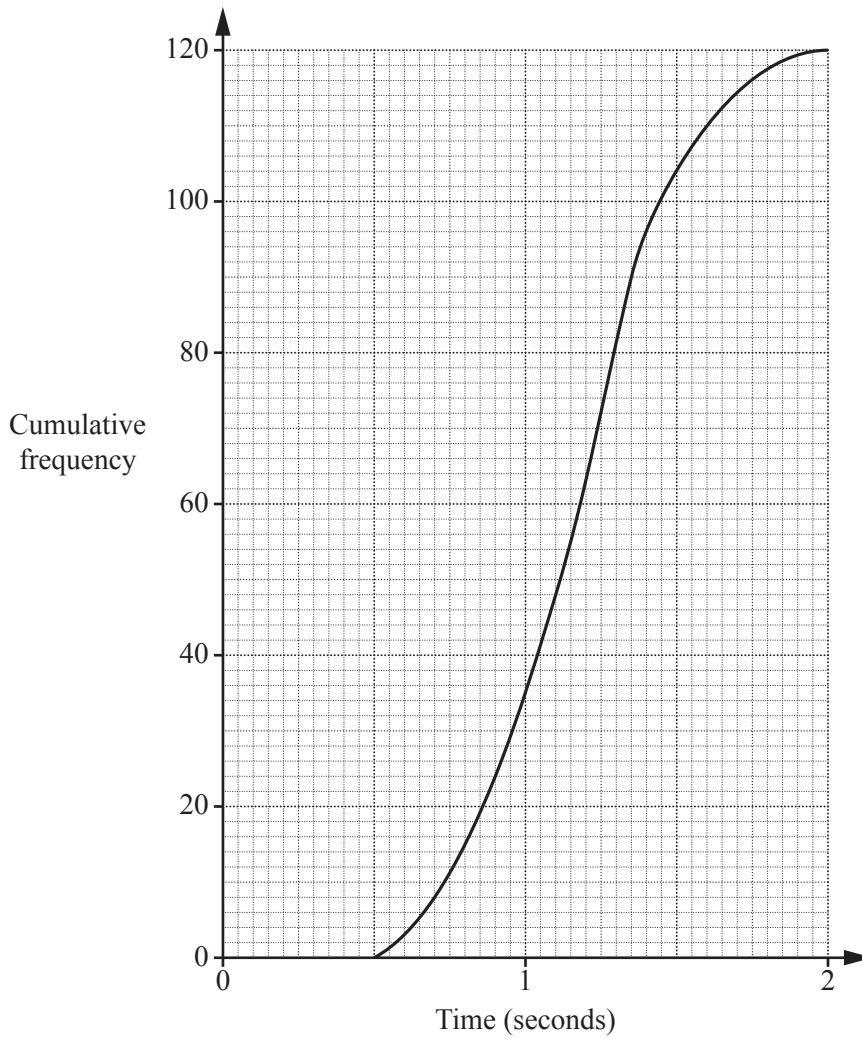
13 Solve the simultaneous equations.

$$\begin{aligned}4x - 3y &= 14 \\ 2x + y &= -3\end{aligned}$$

Answer  $x =$  .....

$y =$  ..... [3]

- 14 The times taken by each of 120 runners to react to the starting gun were recorded. The cumulative frequency curve summarises the results.



- (a) Find the upper quartile.

Answer ..... s [1]

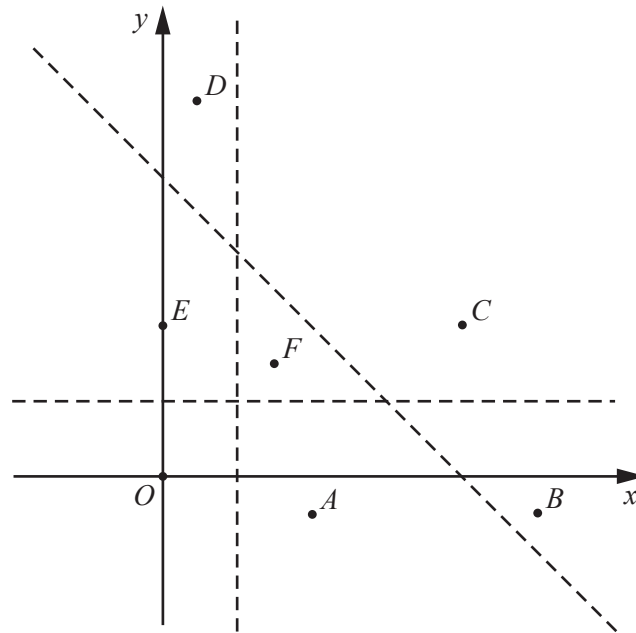
- (b) Find the 40th percentile.

Answer ..... s [1]

- (c) Find the number of students who took less than 1.5 seconds.

Answer ..... [1]





The diagram shows the three lines  $x = 1$ ,  $y = 1$  and  $x + y = 4$  and the seven points  $O, A, B, C, D, E$  and  $F$ .

- (a) Which of these seven points lie in the region defined by  $x + y > 4$ ?

*Answer* ..... [1]

- (b) Which one of these seven points lies in the region defined by

$$x < 1, y > 1 \text{ and } x + y < 4?$$

*Answer* ..... [1]

- (c) Given that  $O$  is  $(0, 0)$  and  $C$  is  $(4, 2)$ , find the inequality that defines the region below the line that passes through  $O$  and  $C$ .

*Answer* ..... [1]

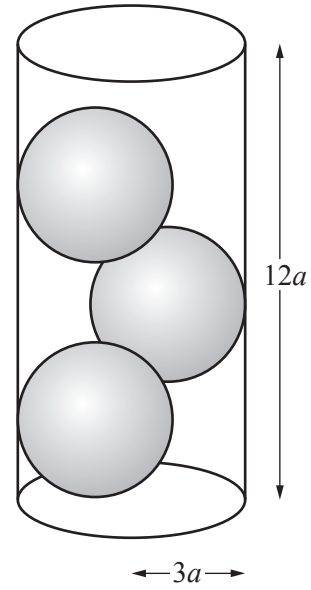
**16 [Volume of a sphere =  $\frac{4}{3}\pi r^3$ ]**

Three spheres, each of radius  $2a$  cm are placed inside a cylinder of radius  $3a$  cm and height  $12a$  cm.

Water is poured into the cylinder to fill it completely.

The volume of water is  $k\pi a^3 \text{ cm}^3$ .

Find the value of  $k$ .



*For  
Examiner's  
Use*

*Answer*  $k = \dots\dots\dots$  [3]

17 (a) Factorise  $25t^2 - 4$ .

Answer ..... [1]

(b) Factorise completely  $6r^2H - 2r^2h$ .

Answer ..... [1]

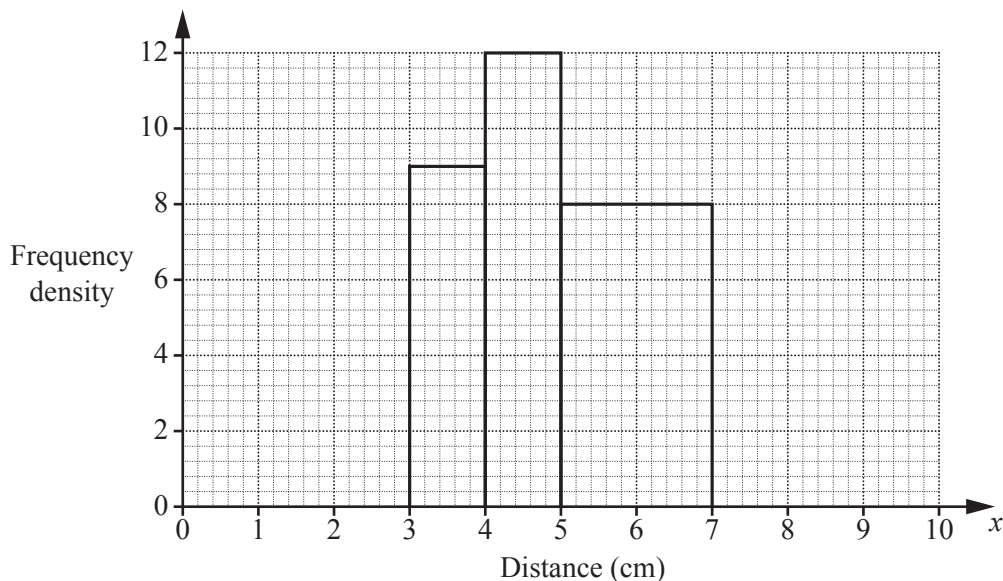
(c) Factorise completely  $8xy + 4x - 6y - 3$ .

Answer ..... [2]

---

- 18 In an experiment with a group of snails, the distance moved in one minute by each snail was recorded.  
Some of the results are shown in the table and illustrated in the histogram.

Distance ( $x$ centimetres)	$2 < x \leq 3$	$3 < x \leq 4$	$4 < x \leq 5$	$5 < x \leq 7$	$7 < x \leq 9$
Frequency	6	9	12	$p$	4



- (a) Use the histogram to find the value of  $p$ .

Answer  $p = \dots\dots\dots$  [1]

- (b) Complete the histogram. [2]

- (c) One snail is chosen at random.

Find the probability that this snail did not move more than 4 cm.

Answer  $\dots\dots\dots$  [1]

19  $P$  is  $(-1, 3)$  and  $Q$  is  $(5, -1)$ .

(a) Find the coordinates of the midpoint of  $PQ$ .

*Answer* (....., .....) [1]

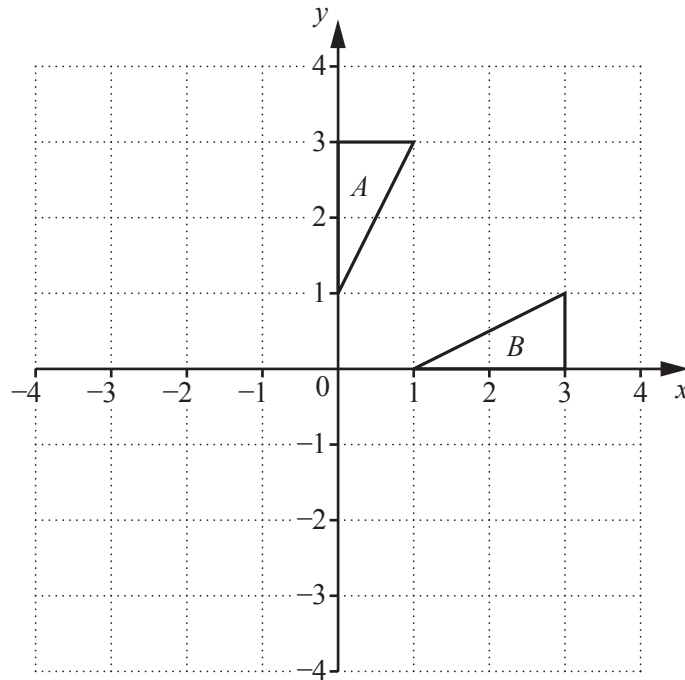
(b) Find the gradient of the line  $PQ$ .

*Answer* ..... [1]

(c) Given that the length of  $PQ = 2\sqrt{n}$  units, where  $n$  is an integer, find the value of  $n$ .

*Answer*  $n =$  ..... [2]

---



The diagram shows triangles  $A$  and  $B$ .

- (a) Describe fully the **single** transformation that maps triangle  $A$  onto triangle  $B$ .

Answer .....

..... [2]

- (b) Triangle  $A$  is mapped onto triangle  $C$  by the transformation  $\mathbf{T}$ .  
 $\mathbf{T}$  is a rotation, centre the origin, through  $270^\circ$  clockwise.

- (i) On the diagram, draw triangle  $C$ . [1]
- (ii) Find the matrix that represents  $\mathbf{T}$ .

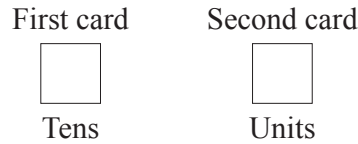
Answer  $\left( \begin{array}{cc} & \\ & \end{array} \right)$  [1]

21



*For  
Examiner's  
Use*

The numbers 2, 3, 3, 4, 4, 4 are written on six cards.  
Two cards are chosen, at random, without replacement, to form a 2-digit number.  
The first card chosen shows the number of Tens.  
The second card chosen shows the number of Units.



Expressing each answer in its simplest form, find the probability that the two cards show

(a) a number greater than 20,

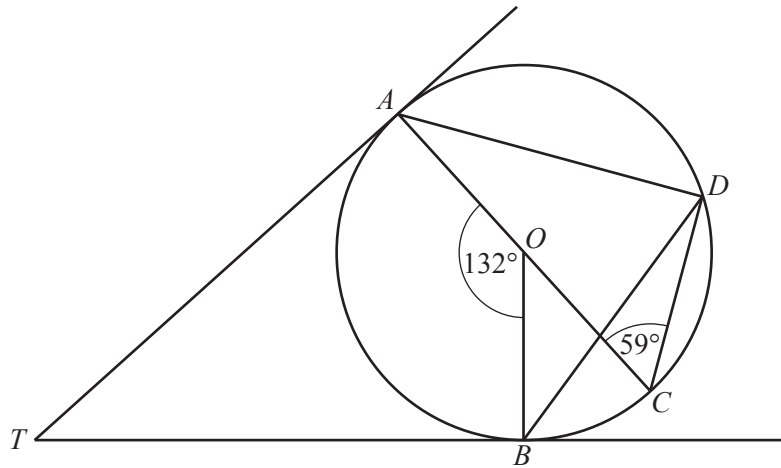
*Answer* ..... [1]

(b) the number 33,

*Answer* ..... [1]

(c) the number 43 or the number 32.

*Answer* ..... [2]



In the diagram, the points  $A$ ,  $B$ ,  $C$  and  $D$  lie on the circle centre  $O$ .  
 $TA$  and  $TB$  are tangents touching the circle at  $A$  and  $B$  respectively.

$\hat{AOB} = 132^\circ$ ,  $\hat{ACD} = 59^\circ$  and  $AOC$  is a straight line.

(a) Find  $\hat{ATB}$ .

Answer  $\hat{ATB} = \dots\dots\dots$  [1]

(b) Find  $\hat{BDA}$ .

Answer  $\hat{BDA} = \dots\dots\dots$  [1]

(c) Find  $\hat{BDC}$ .

Answer  $\hat{BDC} = \dots\dots\dots$  [1]

(d) Find  $\hat{OBD}$ .

Answer  $\hat{OBD} = \dots\dots\dots$  [1]



23 The first four lines of a pattern of numbers are shown below.

$$\text{1st line} \quad 3^2 - 1^2 = 8 \times 1$$

$$\text{2nd line} \quad 5^2 - 1^2 = 8 \times (1 + 2)$$

$$\text{3rd line} \quad 7^2 - 1^2 = 8 \times (1 + 2 + 3)$$

$$\text{4th line} \quad 9^2 - 1^2 = 8 \times (1 + 2 + 3 + 4)$$

(a) Write down the 7th line of the pattern.

*Answer* ..... [1]

(b) Write down an expression, in terms of  $n$ , to complete the  $n$ th line of the pattern.

*Answer* ..... =  $8 \times (1 + 2 + 3 + 4 + \dots + n)$  [1]

(c) Using the  $n$ th line of the pattern, show that  $1 + 2 + 3 + 4 + \dots + n = \frac{n(n+1)}{2}$ .

[2]

24 The diagram at the bottom of the page shows triangle  $ABC$ .

(a) Measure  $\hat{BAC}$ .

Answer ..... [1]

(b) On the diagram, construct the locus of points, **inside** the triangle  $ABC$ , that are

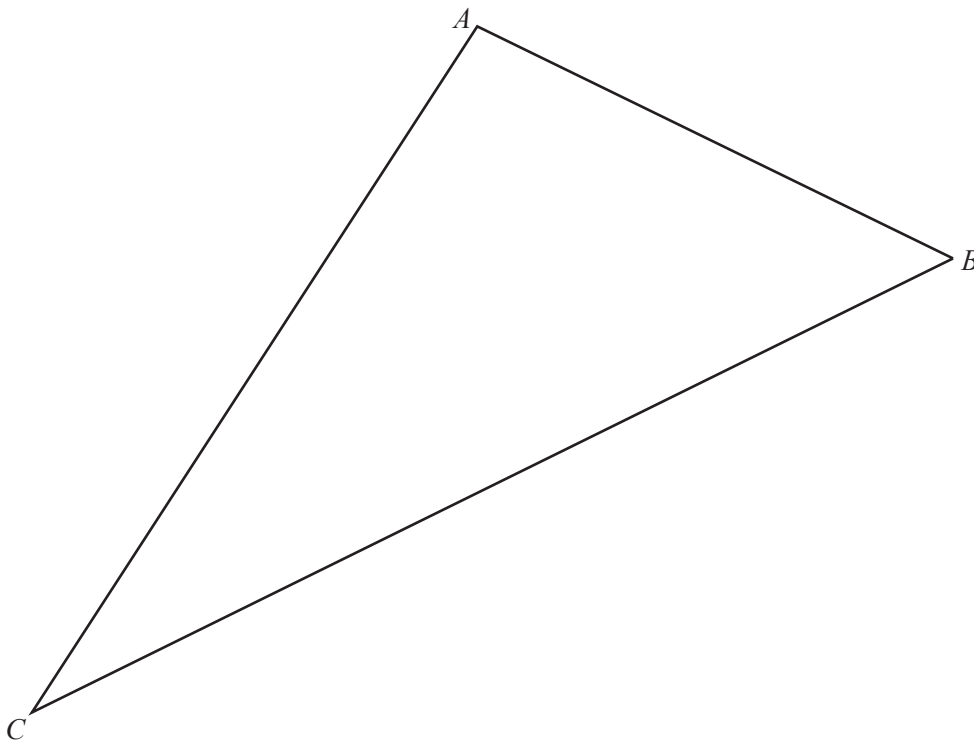
(i) equidistant from  $A$  and  $B$ , [1]

(ii) equidistant from  $AB$  and  $BC$ . [1]

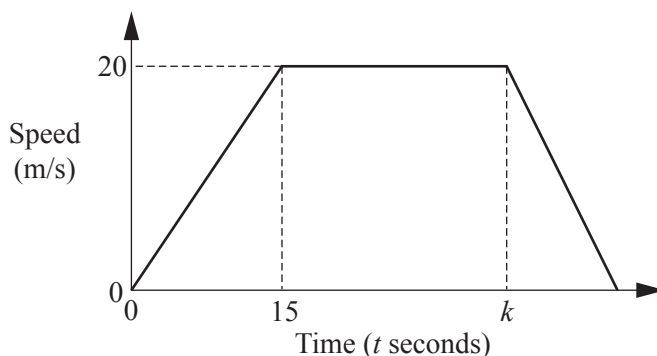
(c) These two loci meet at the point  $P$ .

Label the point  $P$  on the diagram and measure  $CP$ .

Answer  $CP =$  ..... cm [1]



25 The diagram is the speed-time graph of a car's journey.



(a) Find the speed when  $t = 12$ .

Answer ..... m/s [1]

(b) Find the distance travelled by the car from  $t = 0$  to  $t = 15$ .

Answer ..... m [1]

(c) The distance travelled by the car from  $t = 0$  to  $t = k$  is 750 m.

Find  $k$ .

Answer  $k =$  ..... [2]

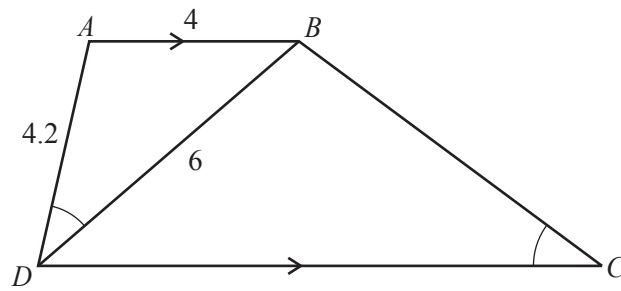
(d) The retardation of the car is  $2 \text{ m/s}^2$ .

Find the number of seconds it takes to slow down and stop.

Answer ..... s [1]

Question 26 is printed on the following page.

26 In the diagram,  $AB$  is parallel to  $DC$  and  $\hat{A}DB = \hat{B}CD$ .



(a) Explain why triangles  $ABD$  and  $BDC$  are similar.

[2]

(b)  $AB = 4$  cm,  $BD = 6$  cm and  $AD = 4.2$  cm.

(i) Calculate  $BC$ .

Answer ..... cm [2]

(ii) Write down the value of  $\frac{\text{area of triangle } ABD}{\text{area of triangle } BDC}$ .

Answer ..... [1]

Permission to reproduce items where third-party owned material protected by copyright is included has been sought and cleared where possible. Every reasonable effort has been made by the publisher (UCLES) to trace copyright holders, but if any items requiring clearance have unwittingly been included, the publisher will be pleased to make amends at the earliest possible opportunity.

University of Cambridge International Examinations is part of the Cambridge Assessment Group. Cambridge Assessment is the brand name of University of Cambridge Local Examinations Syndicate (UCLES), which is itself a department of the University of Cambridge.